

8<sup>èmes</sup> Journées

Fiabilité des  
MATÉRIAUX & DES STRUCTURES

Aix-en-Provence,  
9 et 10 avril 2014



ECOSYSTEMES CONTINENTAUX  
ECCOREV  
ET RISQUES ENVIRONNEMENTAUX



# Influence de la variabilité spatiale des propriétés mécaniques du manteau neigeux sur la stabilité d'une pente

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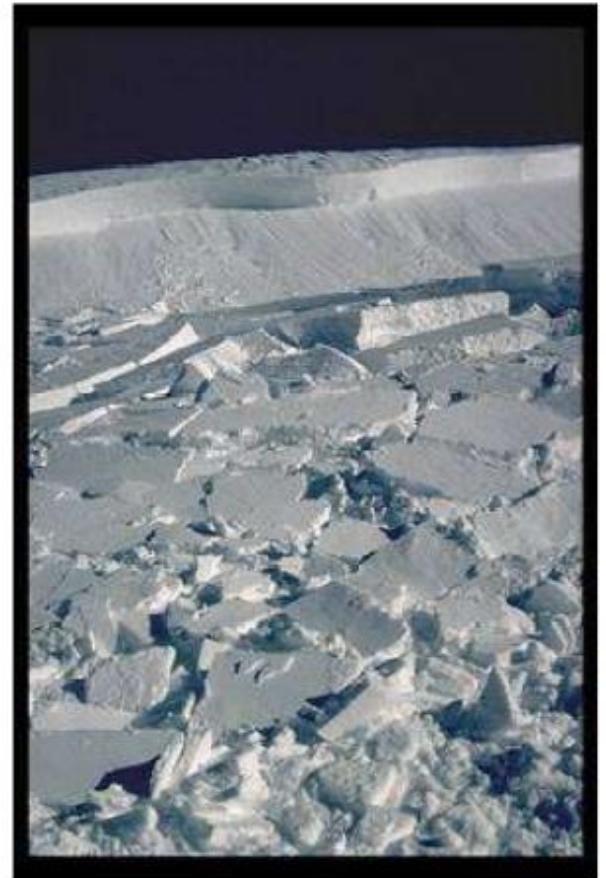


# Context

Slab avalanches result from the failure of a weak snow layer underlying a cohesive snow slab

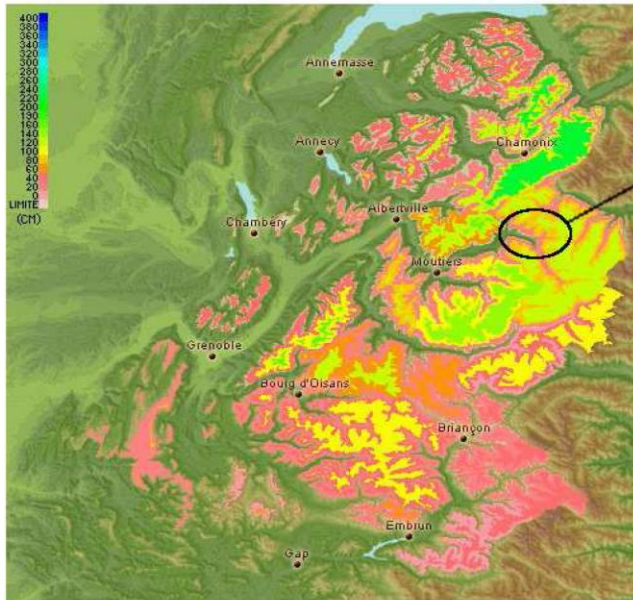


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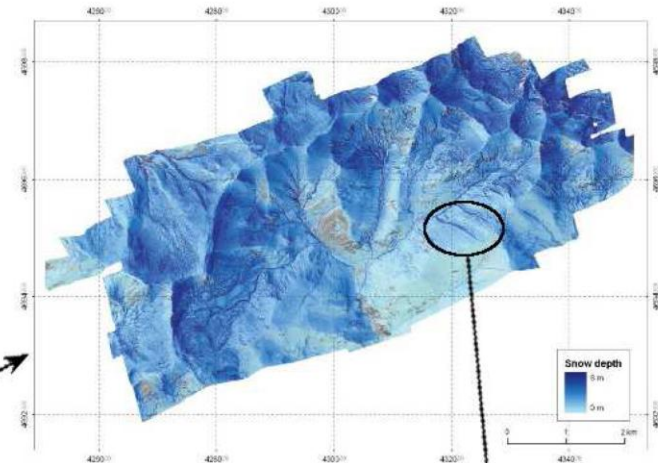


# Context

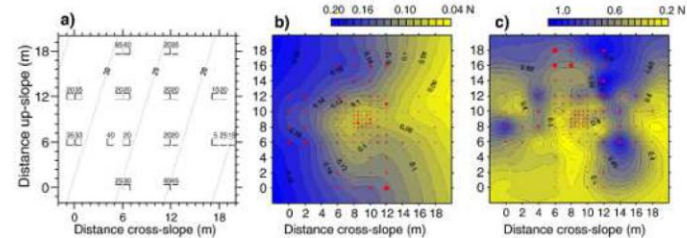
## Complexity of avalanche forecasting due to a multi-scale spatial variability



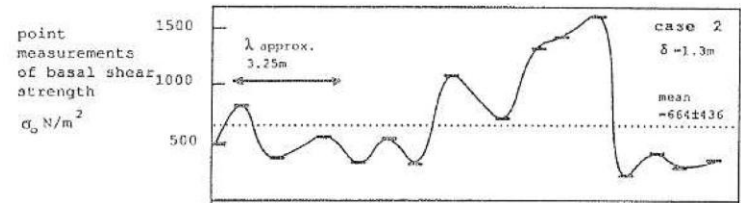
(c) Avalanches-net



From Banos et al 2011



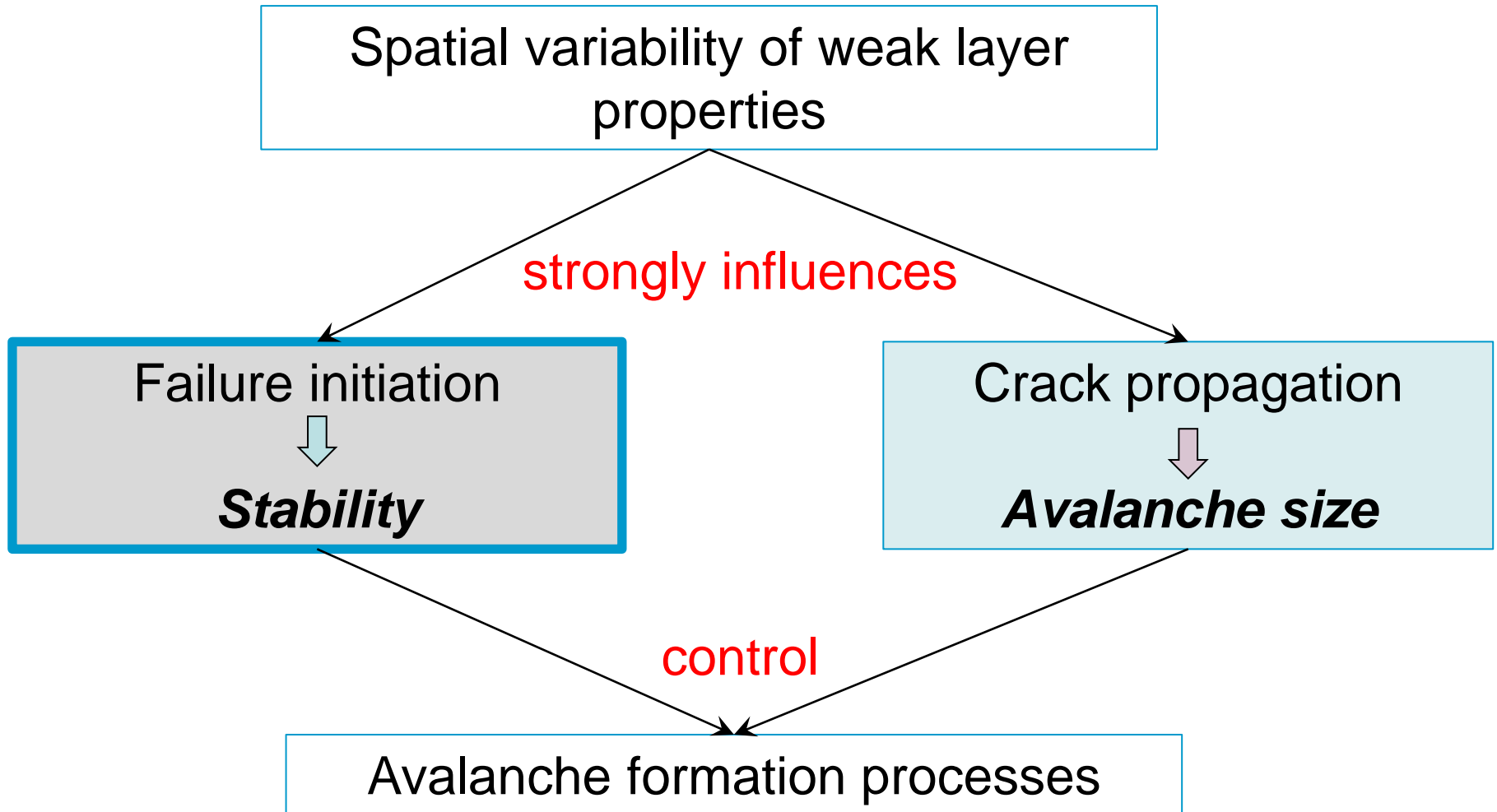
From Schweizer 2008



From Conway and Abrahamson 1988

# Context

Importance of spatial variability for avalanche formation (Schweizer et al., 2008)



# Objective and method

## Objective

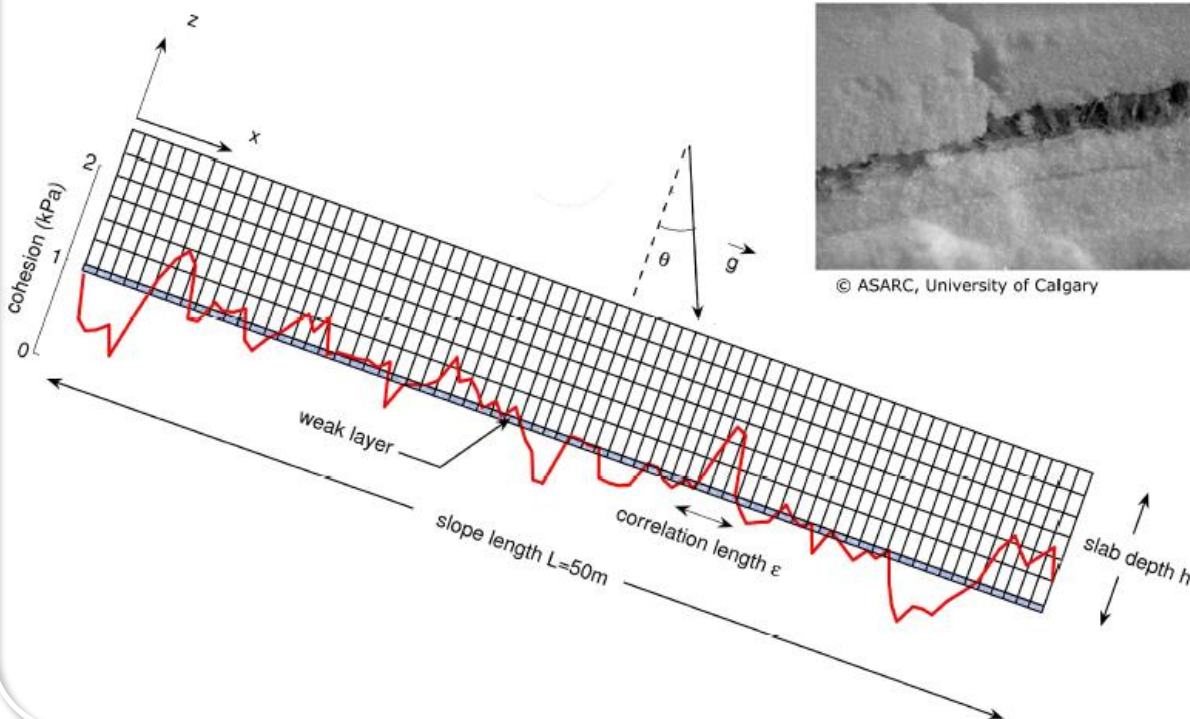
Spatial variability



slope stability

## Method

Mechanically-based statistical model of slab avalanche release  
Gaume et al. (2012, 2013a)



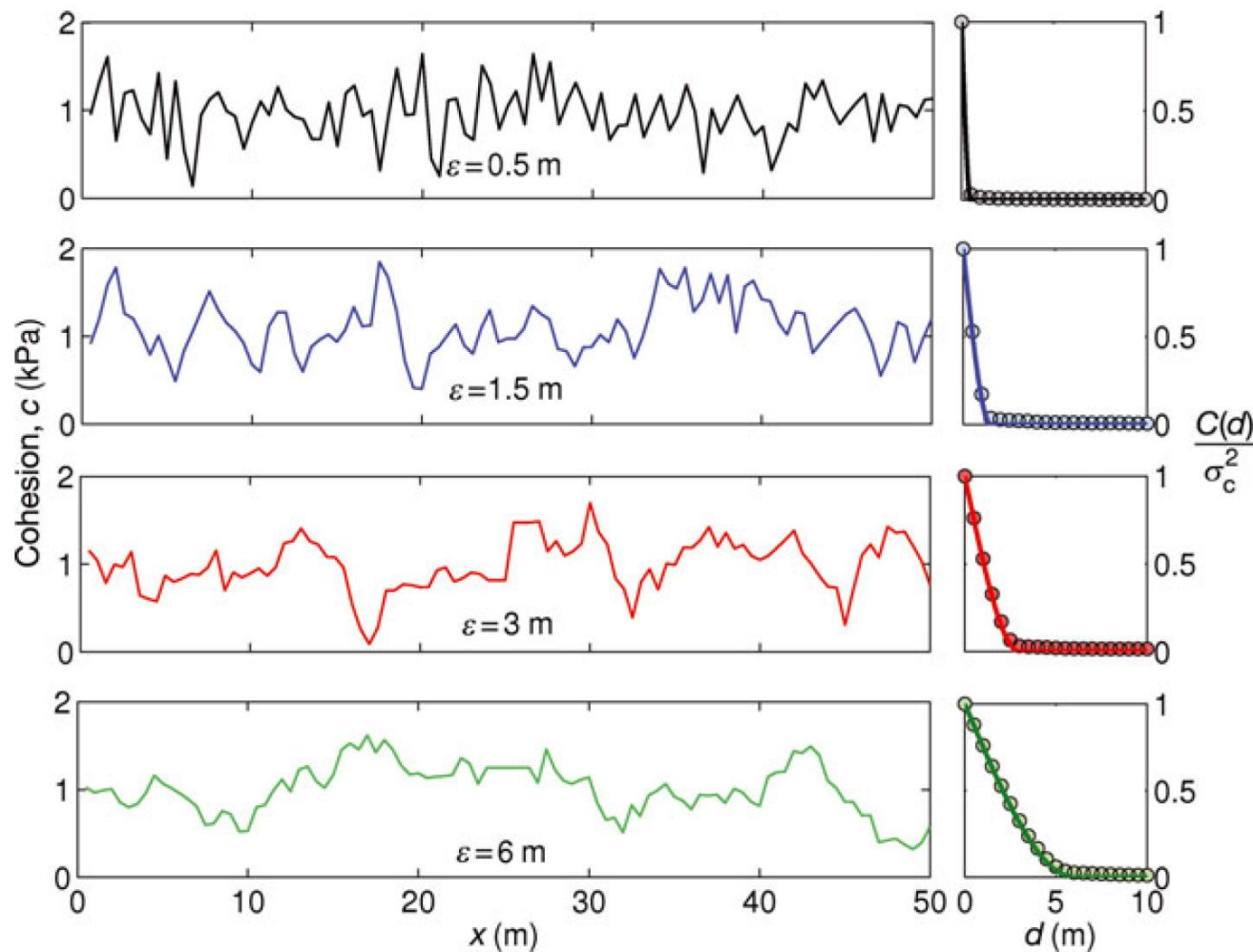
This model takes into account, in particular:

- (1) the spatial variations of WL mechanical properties (shear strength);
- (2) a shear quasi-brittle constitutive law for the WL;
- (3) stress redistribution effects by elasticity of the slab.



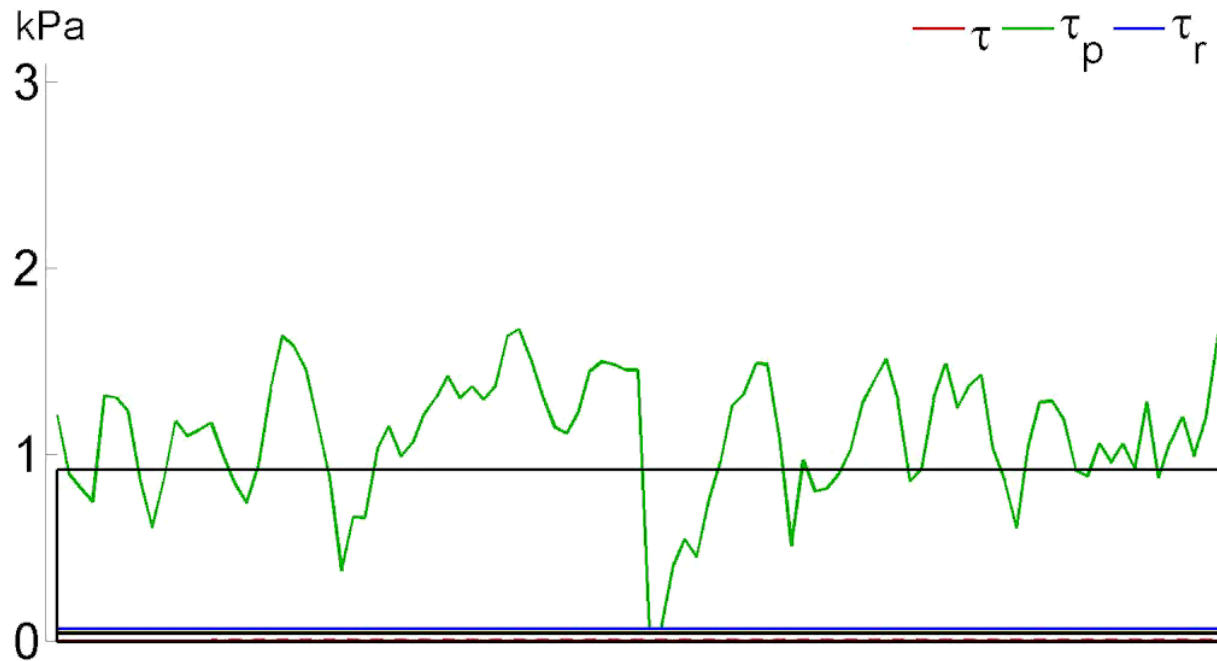
# Objective and method

Spatial variability of the weak-layer cohesion:  
Gaussian distribution with a spherical covariance function



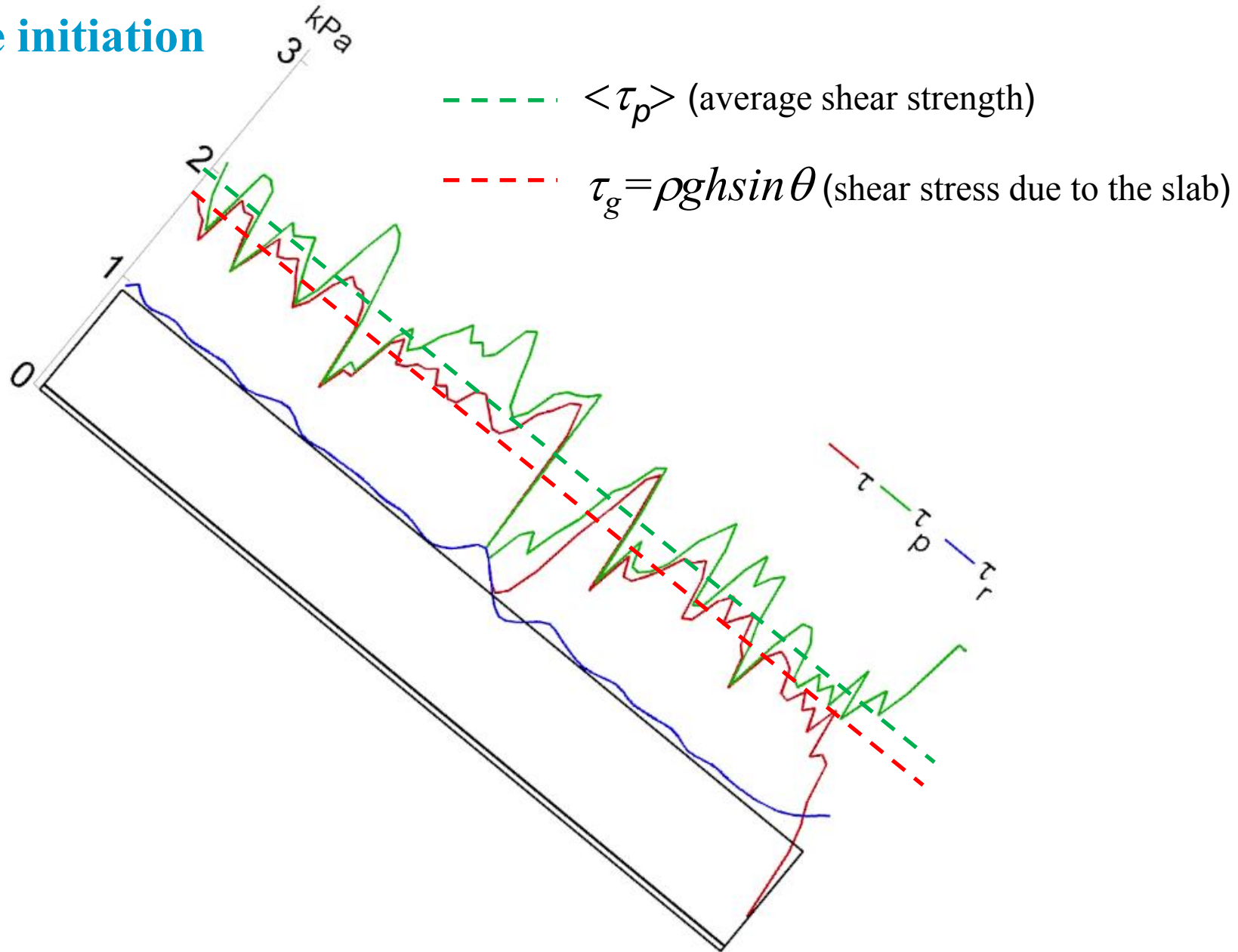
# Illustration

## Illustration: slope stability evaluation



# Illustration

## Failure initiation





# Results

## Avalanche probability evaluation

FE simulations  $\longrightarrow$  Release depth distributions

$$P(h|\theta) = \frac{1}{\sigma_h \sqrt{2\pi}} e^{-\frac{1}{2} \left[ \frac{h - \langle h \rangle}{\sigma_h} \right]^2}$$

$$\langle h \rangle = f_1 \left( \frac{\varepsilon}{h}, \text{CV}, E \right) \frac{\langle c \rangle}{\rho g F}, \quad \sigma_h = \frac{\sigma_c}{\rho g F} \sqrt{f_2 \left( \frac{\varepsilon}{\Lambda}, E \right)}$$

$$F = \sin \theta - \mu \cos \theta, \quad \Lambda = \sqrt{\frac{Eh / (1 - \nu^2)}{k_{WL}}}$$

Avalanche release occurs if the slab depth  $h$  is higher than the critical depth  $h_c$  coming from the mechanical stability criterion:

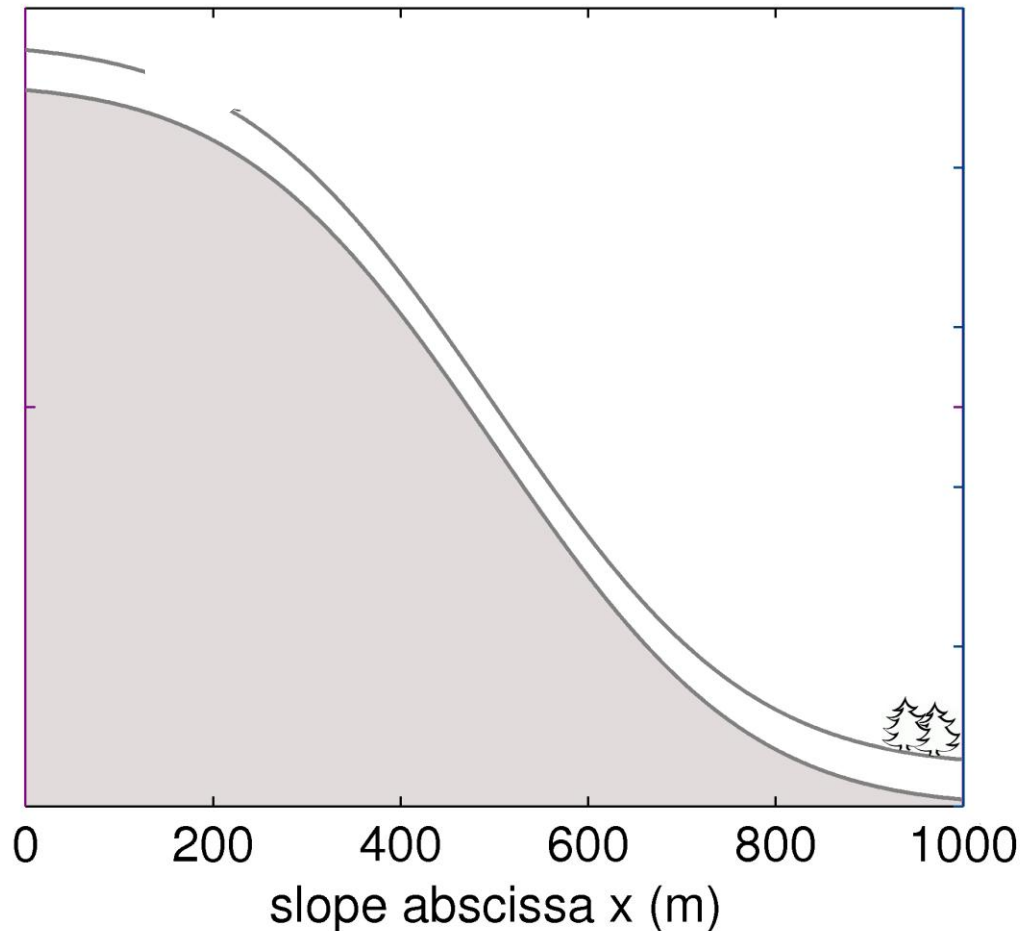
$$P_{aval} = P = P(h_{real} = h \geq h_c) = \int_0^h P(h_c|\theta) dh_c$$

$$\longrightarrow P_{aval} = \frac{1}{2} \left[ 1 + \text{erf} \left( \frac{\rho g h F - f_1 \langle c \rangle}{\sigma_c \sqrt{2 f_2}} \right) \right] \quad \begin{array}{l} f_1 < 1 \\ f_2 < 1 \end{array}$$

# Results

## Slope stability evaluation

$h_z=50\text{cm}$   
 $\rho=250\text{kg/m}^3$   
 $E=1\text{MPa}$   
 $\tau_p=800\text{Pa}$

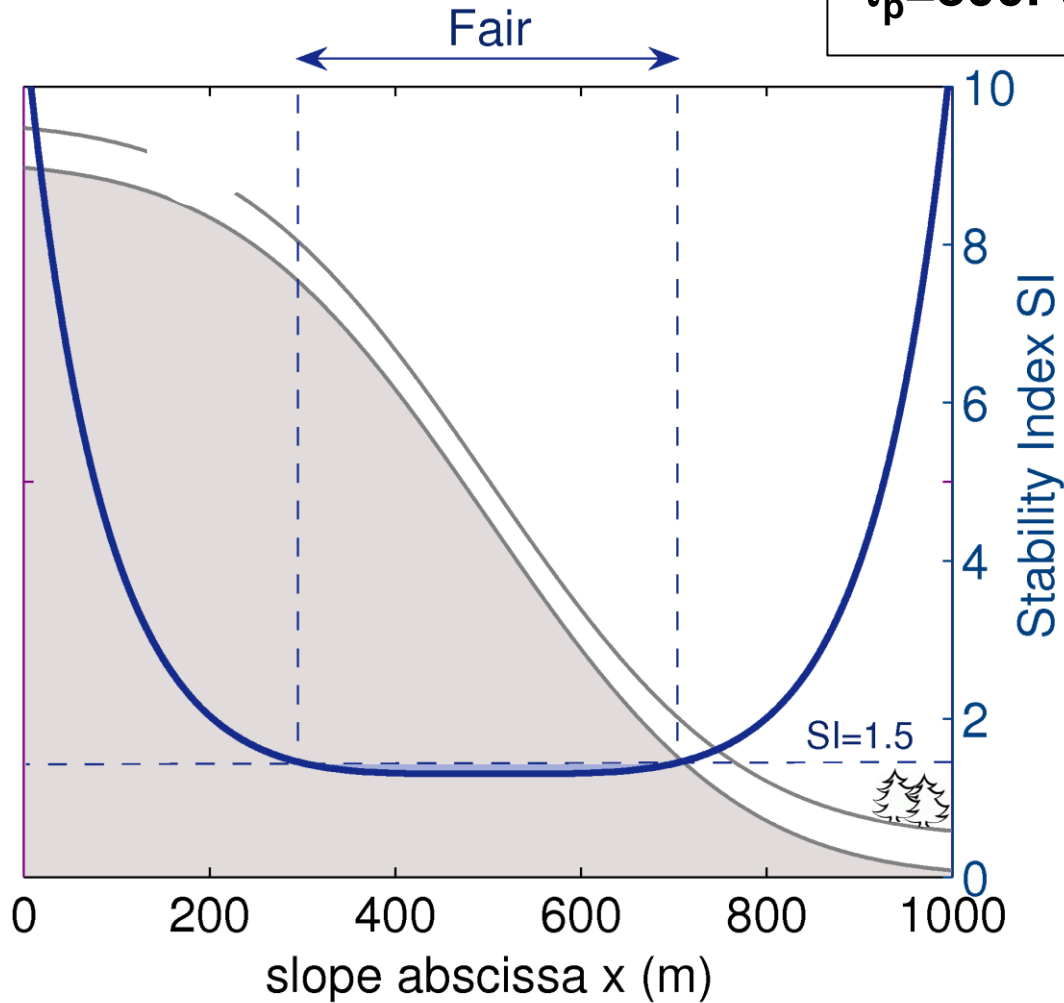


Stability  
index  
SI  
=  
 $\frac{\text{shear strength}}{\text{shear stress}}$   
=  
 $\frac{\tau_p}{\tau_{xz}}$

# Results

## Slope stability evaluation

$h_z=50\text{cm}$   
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Stability index  
 $SI$   
 $=$   
 $\frac{\text{shear strength}}{\text{shear stress}}$   
 $=$   
 $\frac{\tau_p}{\tau_{xz}}$

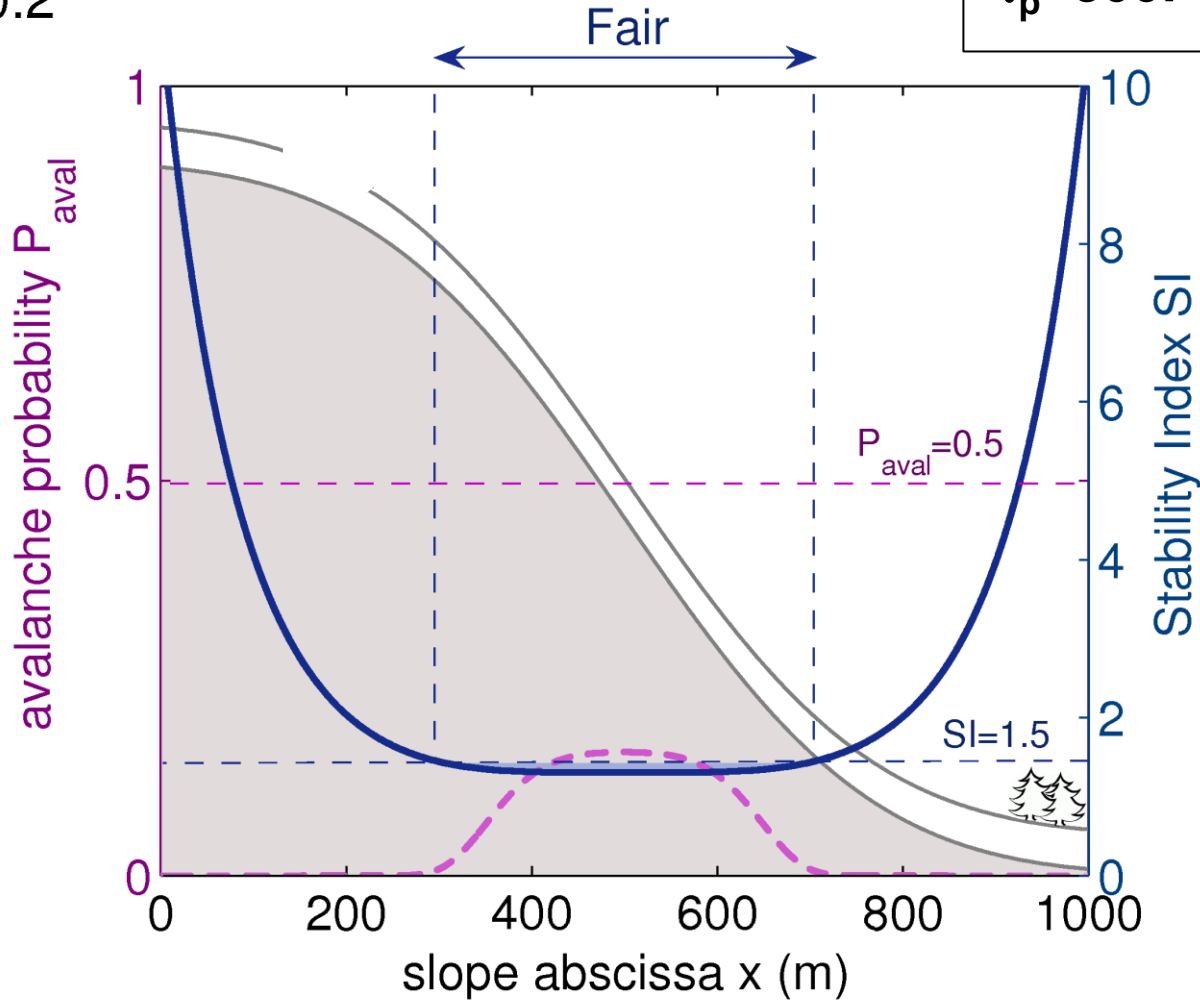
# Results

## Slope stability evaluation

$h_z=50\text{cm}$   
 $\rho=250\text{kg/m}^3$   
 $E=1\text{MPa}$   
 $\tau_p=800\text{Pa}$

--- CV=0.2

$$CV = \frac{\sigma_{\tau_p}}{\langle \tau_p \rangle}$$



$$\begin{aligned}
 \text{Stability index} \\
 SI &= \frac{\text{shear strength}}{\text{shear stress}} \\
 &= \frac{\tau_p}{\tau_{xz}}
 \end{aligned}$$

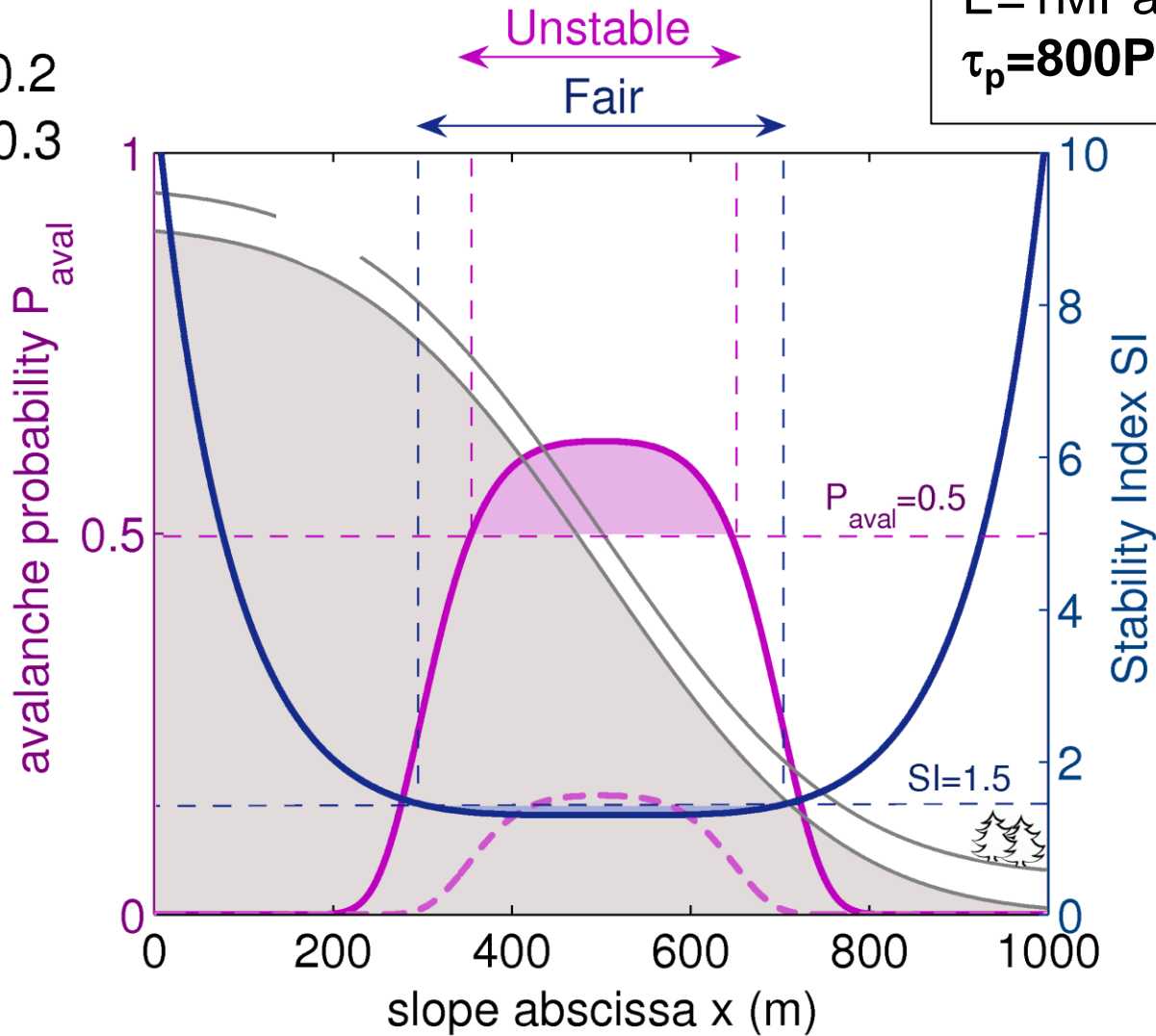
# Results

## Slope stability evaluation

$h_z=50\text{cm}$   
 $\rho=250\text{kg/m}^3$   
 $E=1\text{MPa}$   
 $\tau_p=800\text{Pa}$

- - - CV=0.2  
 — CV=0.3

$$\text{CV} = \frac{\sigma_{\tau_p}}{\langle \tau_p \rangle}$$

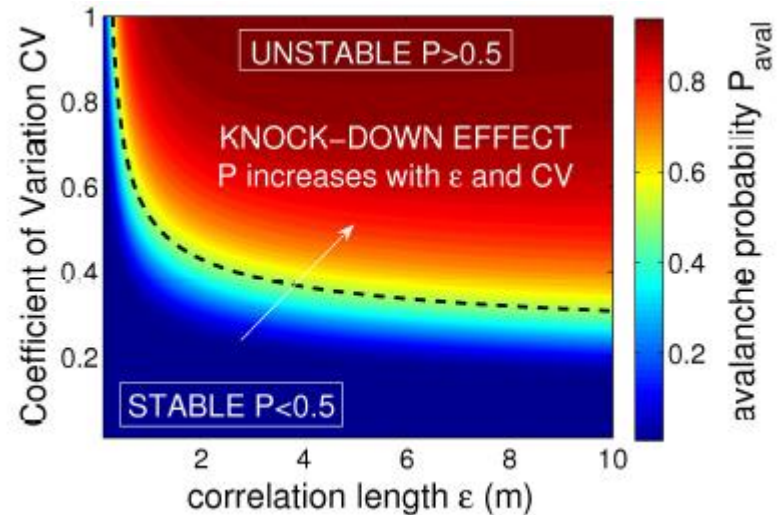
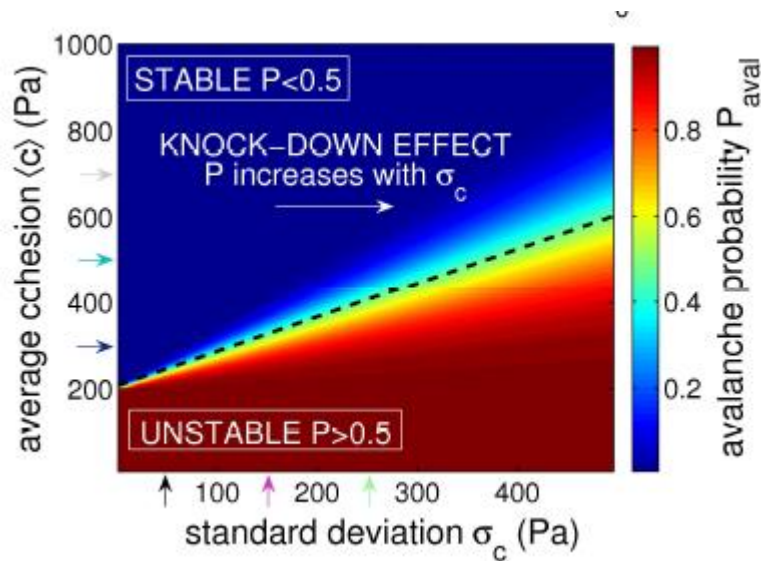
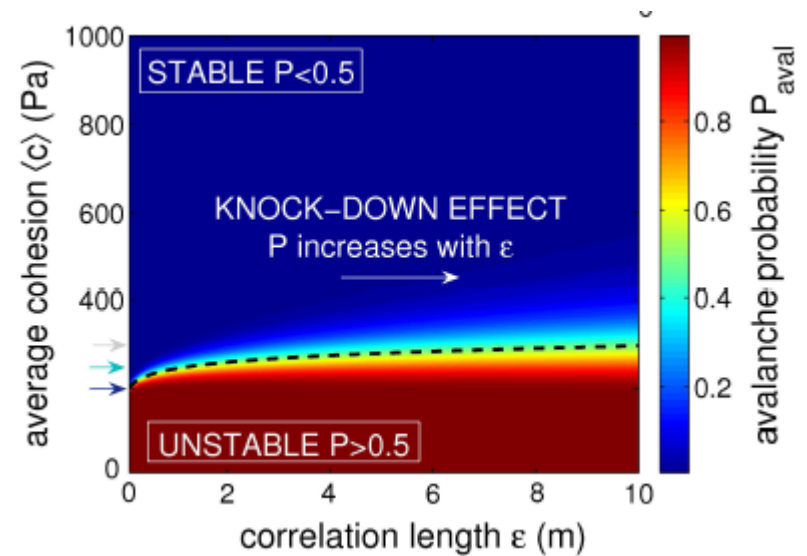


$$\begin{aligned}
 \text{Stability index SI} &= \frac{\text{shear strength}}{\text{shear stress}} \\
 &= \frac{\tau_p}{\tau_{xz}}
 \end{aligned}$$

# Results

## Slope stability evaluation

$$P_{\text{aval}} = \frac{1}{2} \left[ 1 + \operatorname{erf} \left( \frac{\rho g h F - f_1 \langle c \rangle}{\sigma_c \sqrt{2 f_2}} \right) \right]$$





# Conclusions

- **Mechanical-statistical model of the slab-weak layer system**
  - the spatial variations of WL mechanical properties (shear strength);
  - a shear quasi-brittle constitutive law for the WL;
  - stress redistribution effects by elasticity of the slab;

... to study the influence of weak layer shear strength spatial variability

on

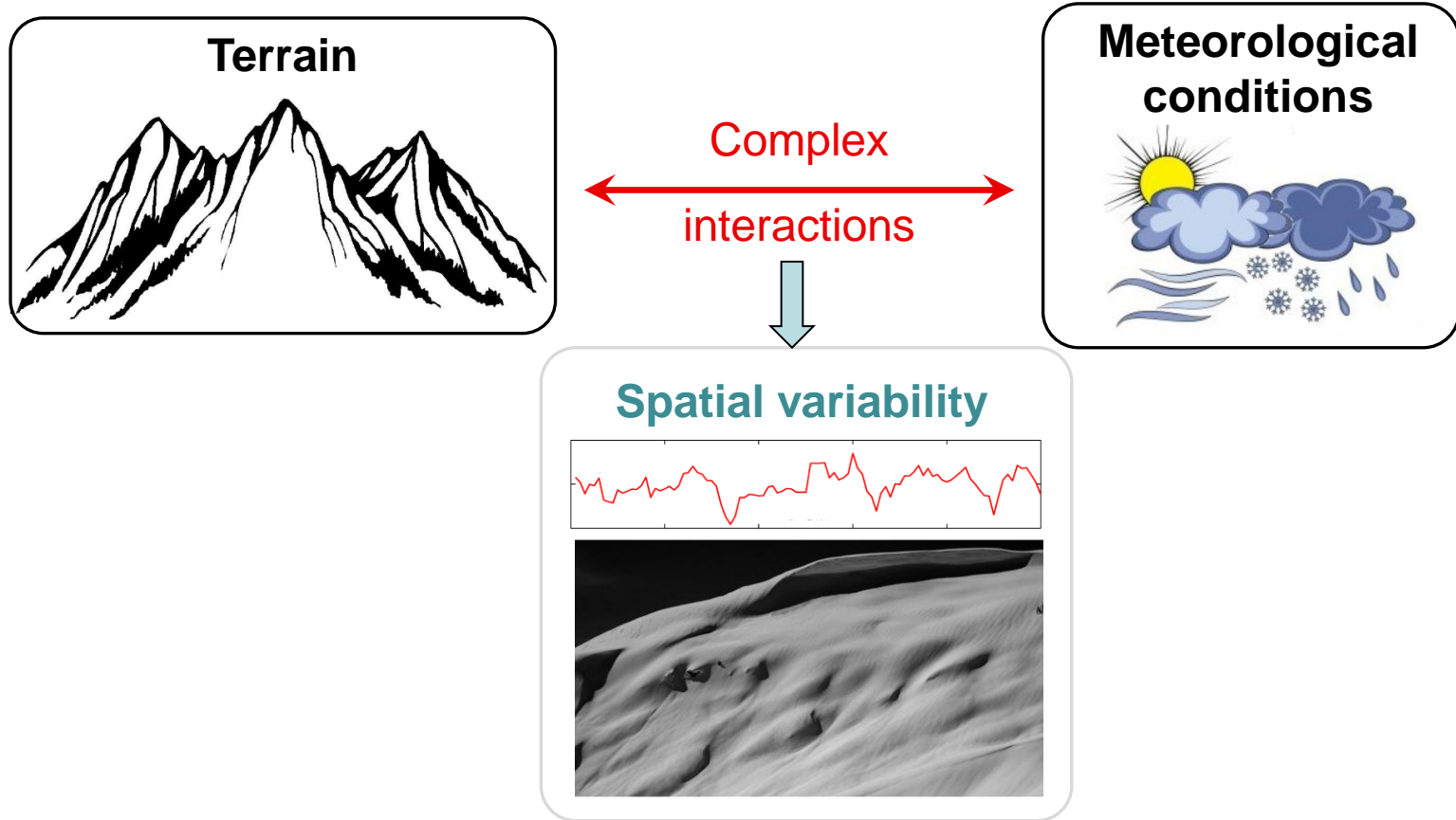
Failure initiation / **snow stability**

Very important “**knock-down**” effect  
on slope stability highlighted

- **An original hazard/geophysically oriented application of the reliability framework**

# Outlooks

- Evaluation of the complex link between spatial variability, terrain and meteorological conditions



- Coupling with extreme snowfall for the regional assessment of avalanche release depths (Gaume et al., 2013b)

# References

Banos, I. et al. (2011). Boletín de la Sociedad Geológica Mexicana. Vol.63, No. 1, pp. 95-107.

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Schweizer, J. et al., 2008. Review of spatial variability of snowpack properties and its importance for avalanche formation. *Cold Regions Science and Technology*, 51, 253-272.

# Thanks for your attention!